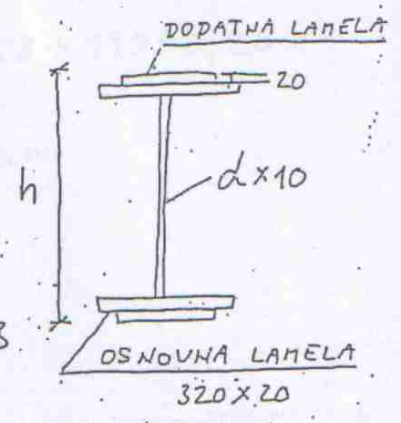
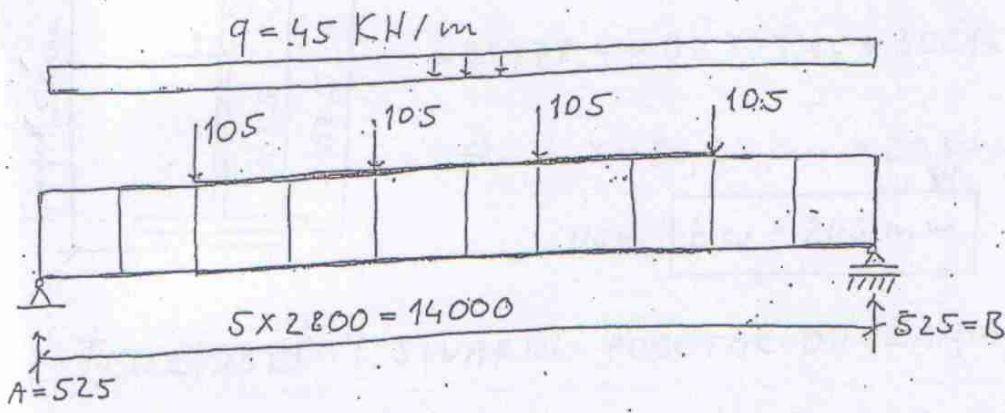


17. JANUAR 2005



$\bar{C}.0361 \rightarrow S235$   
 I SL. OPT.  $\Rightarrow \begin{cases} \sigma_{dop} = 16 \text{ kN/cm}^2 \\ \tau_{dop} = 9 \text{ kN/cm}^2 \end{cases}$   $f_{dop} = L/500 = 2,8 \text{ cm}$

a) Visina  $h$  ZA ISTOVREMENO ISKOKRIŠĆENJE NORMALNOG NAPONA I UGIBA U SREDINI NOSAČA

$A = B = \frac{1}{2} (105 \cdot 4 + 45 \cdot 14) = 525 \text{ kN}$

$M = M_{max} = 525 \cdot 7 - 105 \cdot (2,8 + 1,4 + 1,4) - 45 \cdot \frac{7^2}{2} = 1984,5 \text{ kNm}$

$W_{dop} = \frac{M}{\sigma_{dop}} = \frac{1984,5 \cdot 10^2}{16} = 12403,13 \text{ cm}^3 = \frac{I_x}{h/2} \Rightarrow I_x = 6201,6h$

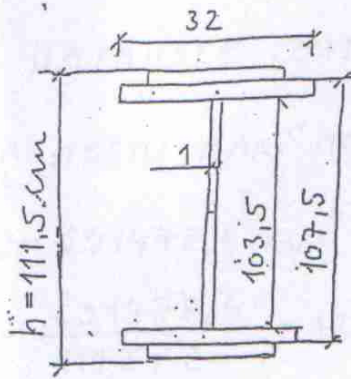
$f_1 = \frac{5}{384} \frac{q l^4}{EI}$   $f_2 = \frac{F \cdot l^3}{15,87 EI}$   $f = f_1 + f_2$

$2,8 = \frac{5}{384} \frac{45 \cdot 10^2 \cdot (1400)^4}{21000 I} + \frac{105 \cdot (1400)^3}{15,87 \cdot 21000 I} \Rightarrow 2,8 = \frac{1071875}{I} + \frac{864524,3}{I}$

$2,8 = \frac{1071875 + 864524,3}{6201,6h} \Rightarrow h = 111,51 \text{ usv. } \boxed{h = 111,5 \text{ cm}}$

POTREBNA ŠIRINA LAMELA AKO IM JE DEBLJINA 20 mm?

$I_x = 6201,6h = 6201,6 \cdot 111,5 = 691478,4 \text{ cm}^4$



$$I_x = \frac{1}{12} \cdot 1 \cdot 103,5^3 + 2 \cdot (52,75^2 \cdot 32 \cdot 2 + 54,75^2 \cdot X \cdot 2) \quad (2)$$

$$691478,4 = 92393,16 + 356168 + 11990,25 X$$

$$\Rightarrow X = 20,26 \text{ cm} = 203 \text{ mm}$$

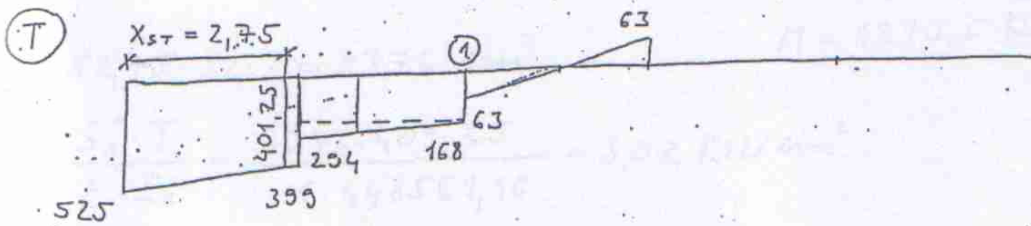
$$\text{USV. } b_{fd} = 205 \text{ mm}$$

c) TEORIJSKI I STVARNI POČETAK OJAČANJA

$$\text{OSNOVNI PRESEK: } I_x = \frac{1}{12} \cdot 103,5^3 + 2 \cdot (52,75^2 \cdot 32 \cdot 2) = 448561,16 \text{ cm}^4$$

$$W_{osn} = \frac{I_x}{h/2} = \frac{448561,16}{107,5/2} = 8345,32 \text{ cm}^3$$

$$\sigma_{dop} = 16 = \frac{M}{W_{osn}} \Rightarrow M = 16 \cdot 8345,32 \cdot 10^{-2} = 1335,25 \text{ kNm}$$



$$\frac{525 + 399}{2} \cdot 2,8 = 1293,6 + 168 \cdot X + \frac{126 + 126 + 45 \cdot X}{2} \cdot X = 1335,25$$

$$\Rightarrow 1293,6 + 168X + 126X - 22,5X^2 = 1335,25$$

$$X^2 - 13,067X + 1,851 = 0 \Rightarrow X_{1,2} = \frac{13,067 \pm \sqrt{13,067^2 - 4 \cdot 1,851}}{2} = \begin{cases} 12,92 \text{ m} \\ 0,14 \text{ m} \end{cases}$$

$$x_{TE} = 2,8 + 0,14 = 2,94 \text{ m} \quad X_{2TE} = 11,06 \text{ m}$$

$$x_{ST} = 2,94 - \frac{0,32}{2} = 2,78 \text{ m} \quad X_{2ST} = 11,06 + \frac{0,32}{2} = 11,22 \text{ m}$$

$$\text{USVAJA SE } X_{1ST} = 2,75 \text{ m} \quad \text{I} \quad X_{2ST} = 11,25 \text{ m}$$

2) NAPONSKE KONTROLE U KARAKTERISTIČNIM PRESECIMA

NA MESTU MAX. MOMENTA. (max M = 1984,5 KNm, T<sub>0,2g</sub> = 0)

I<sub>x</sub> = 691478,4 cm<sup>4</sup>

σ =  $\frac{\max M}{W} = \frac{1984,5 \cdot 10^2}{12403,2} = 16 \text{ KN/cm}^2$

W =  $\frac{691478,4}{111,5/2} = 12403,2 \text{ cm}^3$

= σ<sub>dop</sub>

NA MESTU T<sub>max</sub> (T<sub>max</sub> = 525 KN, M = 0)

σ =  $\frac{T_{max} S_x}{t \cdot I_x}$

S<sub>x</sub> = 52,75 · 2 · 32 + 51,75 · 1 ·  $\frac{51,75}{2}$  = 4715 cm<sup>3</sup>

I<sub>x</sub> = 448561,16 cm<sup>4</sup>

σ =  $\frac{525 \cdot 4715}{1 \cdot 448561,16} = 5,52 \text{ KN/cm}^2 < \tau_{dop}$

NA MESTU OJACANJA (T = 401,25 KN, M =  $\frac{401,25 + 525}{2} \cdot 2,75$ )

S<sub>x</sub> = 52,75 · 32 · 2 = 3376 cm<sup>3</sup>

M = 1273,6 KNm

σ =  $\frac{S_x \cdot T}{t \cdot I_x} = \frac{3376 \cdot 401,25}{1 \cdot 448561,16} = 3,02 \text{ KN/cm}^2$

τ =  $\frac{1273,6 \cdot 10^2}{448561,16} \cdot 51,75 = 14,69 \text{ KN/cm}^2$

σ<sub>1</sub> =  $\sqrt{\sigma^2 + 3\tau^2} = \sqrt{3,02^2 + 3 \cdot 14,69^2} = 15,6 \text{ KN/cm}^2 < \sigma_{dop}$

NA MESTU TAČKE ① (T = 168 KN, M =  $\frac{525 + 399}{2} \cdot 2,8 + \frac{274 + 168}{2} \cdot 2,8$ )

S<sub>x</sub> = 3376 + 52,75 · 20,5 · 2 = 5620,75 cm<sup>3</sup>

M = 1940,4 KNm

I<sub>x</sub> = 691478,4 cm<sup>4</sup>

σ =  $\frac{5620,75 \cdot 168}{1 \cdot 691478,4} = 1,37 \text{ KN/cm}^2$

τ =  $\frac{1940,4 \cdot 10^2}{691478,4} \cdot 51,75 = 14,52 \text{ KN/cm}^2$

σ<sub>u</sub> =  $\sqrt{\sigma^2 + \tau^2} = \sqrt{1,37^2 + 14,52^2} = 14,71 \text{ KN/cm}^2 < \sigma_{dop}$



e) KONTROLA NOSAČA NA BOČNO TORZIONO IZVIJANJE

(GORNJI POJAS JE BOČNO PRIDRŽAN U PETINAMA RASPONA)

$$I_y = \frac{1}{12} \cdot 2 \cdot 32^3 + \frac{1}{12} \cdot 2 \cdot 20,5^3 = 6897,19 \text{ cm}^4$$

$$A_f = 2 \cdot (20,5 + 32) = 105 \text{ cm}^2$$

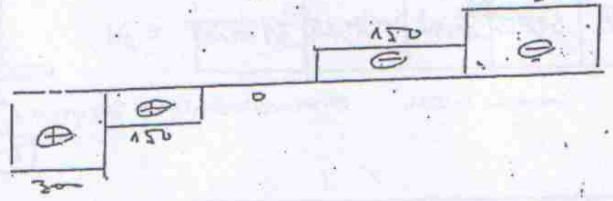
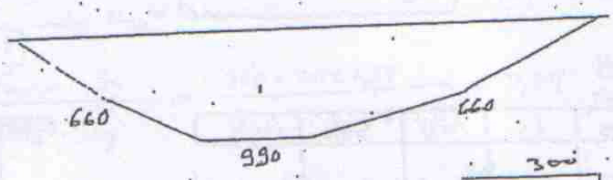
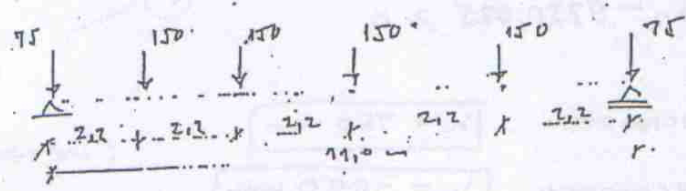
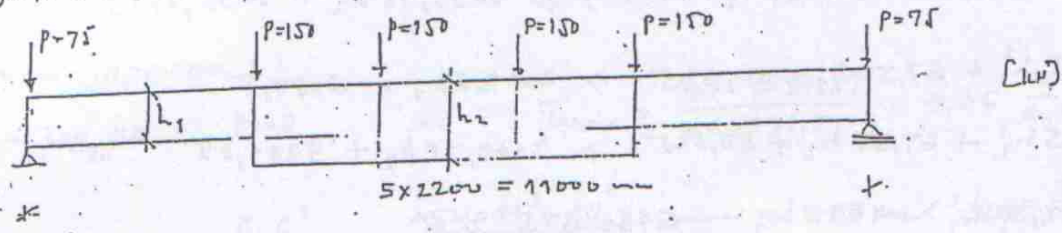
$$\bar{i}_y = \sqrt{\frac{I_y}{A_f}} = \sqrt{\frac{6897,19}{105}} = 8,11 \text{ cm} \quad l_z = 2,8 \text{ m} = 280 \text{ cm}$$

$$\lambda_y = \frac{l_z}{\bar{i}_y} = \frac{280}{8,11} = 34,52 < 40 \Rightarrow \text{NEMA OPASNOSTI OD BOČNO TORZIONOG IZVIJANJA}$$

Носач статичког система просте греде распона 11,0м интересан је системом концентрисаних сила као што је приказано на слици

Носач је применљиве масине са ножицама  $300 \times 15 \text{ mm}$  и ребром дебљине  $10 \text{ mm}$ . Одредити висине ребра  $h_1$  и  $h_2$  и извршити све потребне

натпоне контроле у карактеристичним пресецима: димензионисати угачне шавове за безу ножица и ребра. Извршити контролу туба ( $f_{\text{дор}} = 21300$ ) и контролу стабилности ребра на избочавање у пољу по основу: Сливом материјал  $\text{С-0367 (S235)}$  - I случај оптерећења



Заређујемо  $L_1$  и  $L_2$ :

$$w = \frac{M_{\text{max}}^1}{W_y^1} \leq 16 \Rightarrow \frac{M_{\text{max}}^1}{I_y^1} \cdot \frac{L_1}{2} \leq 16$$

$$w = \frac{M_{\text{max}}^2}{W_y^2} \leq 16 \Rightarrow \frac{M_{\text{max}}^2}{I_y^2} \cdot \frac{L_2}{2} \leq 16$$

$$I_y^1 = \frac{1}{12} h_1^3 + 2 \cdot 300 \cdot 15 \cdot \left( \frac{h_1 + 15}{2} \right)^2$$

$$I_y^2 = \frac{1}{12} h_2^3 + 2 \cdot 300 \cdot 15 \cdot \left( \frac{h_2 + 15}{2} \right)^2$$

$$I_y^1 = \frac{1}{12} h_1^3 + 90 (0,5 h_1 + 0,75)^2$$

$$I_y^2 = \frac{1}{12} h_2^3 + 90 (0,5 h_2 + 0,75)^2$$

$$W(h) = \frac{I(h)}{\frac{h+3}{2}}$$

$$w = \frac{M_{\text{max}}}{W}$$

$$W(h) \geq W_{\text{доп}}$$

$$W(h_1) \geq W_{dip}^1 \Rightarrow \frac{I(h_1)}{h_1+3} \geq \frac{660 \cdot 10^4}{16}$$

$$W(h_1) \geq W_{dip}^2 \Rightarrow \frac{I(h_2)}{h_2+3} \geq \frac{990 \cdot 10^2}{16}$$

$$I(h_1) \geq 4125 \cdot \frac{h_1+3}{2} \Rightarrow \frac{1}{12} h_1^3 + 90 \cdot (0,5h_1 + 0,75)^2 \geq 2062,5 \cdot (h_1+3)$$

$$I(h_2) \geq 6187,5 \cdot \frac{h_2+3}{2} \Rightarrow \frac{1}{12} h_2^3 + 90 \cdot (0,5h_2 + 0,75)^2 \geq 3093,75 \cdot (h_2+3)$$

$$\frac{1}{12} h_1^3 + 90 \cdot (0,5h_1)^2 + 2 \cdot 0,75 \cdot 0,5h_1 + 0,75^2 \geq 2062,5 h_1 + 2062,5 \cdot 3$$

$$\frac{1}{12} h_1^3 + 22,5 h_1^2 + 67,50 h_1 + 50,625 \geq 2062,5 h_1 + 6187,5$$

$$\frac{1}{12} h_1^3 + 22,5 h_1^2 - 1995 h_1 - 6136,875 \geq 0$$

$$\frac{1}{12} h_2^3 + 90 \cdot (0,5h_2)^2 + 2 \cdot 0,75 \cdot 0,5h_2 + 0,75^2 \geq 3093,75 h_2 + 3093,75 \cdot 3$$

$$\frac{1}{12} h_2^3 + 22,5 h_2^2 + 67,50 h_2 + 50,625 \geq 3093,75 h_2 + 9281,25$$

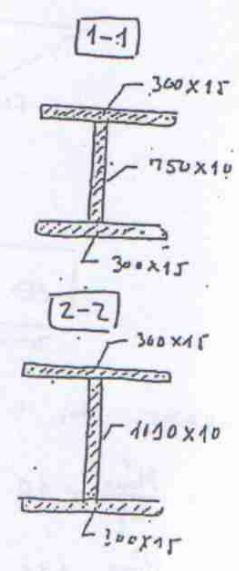
$$\frac{1}{12} h_2^3 + 22,50 h_2^2 - 3026,25 h_2 - 9230,625 \geq 0$$

$$h_1 \geq 72,79 \text{ cm} \Rightarrow \text{выбирается } h_1 = 750 \text{ мм}$$

$$h_2 \geq 100,89 \text{ cm} \Rightarrow \text{выбирается } h_2 = 1050 \text{ мм}$$

A	$I_y$	$I_z$	$W_y$	$W_z$	$i_y$	$i_z$	$S_{y,0}$	$S_z$
165	166831,87	6750	4277,74	450	31,80	6,40	1721,25	2424,37

A	$I_y$	$I_z$	$W_y$	$W_z$	$i_y$	$i_z$	$S_{y,0}$	$S_z$
191	322249,04	6750	6197,10	450	41,07	5,94	2306,25	3581,37



она меньше:

$$\frac{M_{max}}{W} = \frac{660 \cdot 10^2}{4277,74} = 15,43 \frac{\text{кН}}{\text{см}^2} < 16,0 \frac{\text{кН}}{\text{см}^2}$$

$$\frac{M_{max}}{I_y} \cdot \frac{d}{2} = \frac{660 \cdot 10^2}{166831,87} \cdot \frac{75}{2} = 14,83 \frac{\text{кН}}{\text{см}^2}$$

$$\sqrt{6,1^2 + 3\tau_1^2} = 15,77 \frac{\text{кН}}{\text{см}^2}$$

$$\tau_{max,1} = \frac{T_{max} S_y}{I_y \cdot t_w} = \frac{300 \cdot 2424,37}{166831,87 \cdot 1} = 4,36 < 9$$

$$\tau_1 = \frac{T_{max} S_{y,0}}{I_y \cdot t_w} = \frac{300 \cdot 1721,25}{166831,87 \cdot 1} = 3,09$$



$$\sigma_{\max}^{z-z} = \frac{M_{\max}}{W} = \frac{990 \cdot 10^2}{6197,10} = 15,97 \frac{\text{кН}}{\text{см}^2} < 16,0 \frac{\text{кН}}{\text{см}^2}$$

$$\tau_{\max}^{z-z} = \frac{T_{\max} \cdot S_y}{I_y \cdot t_w} = \frac{150 \cdot 3581,37}{322249,04 \cdot 1} = 1,67 \frac{\text{кН}}{\text{см}^2} < 9,0 \frac{\text{кН}}{\text{см}^2}$$

$$\sigma_1 = \frac{M_{\max}}{I_y} \cdot \frac{d}{2} = \frac{990 \cdot 10^2}{322249,04} \cdot \frac{101}{2} = 15,51 \frac{\text{кН}}{\text{см}^2}$$

$$\tau_1 = \frac{T_{\max} \cdot S_{y10}}{I_y \cdot t_w} = \frac{150 \cdot 2306,25}{322249,04 \cdot 1} = 1,073 \frac{\text{кН}}{\text{см}^2}$$

$$\sigma_{\text{ср}} = \sqrt{\sigma_1^2 + 3\tau_1^2} = 15,62 \frac{\text{кН}}{\text{см}^2} < 16,0 \frac{\text{кН}}{\text{см}^2}$$

ОСНОВНЫЙ ПРЭСЕК:

$$T_{\max} = 300 \text{ кН}, M=0 \Rightarrow T_{\max} = \frac{300 \cdot 2424,37}{166831,87 \cdot 1} = 4,36 \frac{\text{кН}}{\text{см}^2} < 9,0 \frac{\text{кН}}{\text{см}^2}$$

$$\text{УГИБ: } f = \frac{F \cdot l^3}{K_f \cdot EI} = \frac{150 \cdot 11^3 \cdot 10^5}{15,87 \cdot 21000 \cdot 166831,87} = 3,59 \text{ см} < f_{\text{доп}} = \frac{1100}{3} = 3,65$$

ЗБИРКА  
889

УГЛОНИ ШАРОВЫХ:

ПРЕДПОСТАВКА  $\min a_w = 3 \text{ мм}$

КНИГА СТР. 188

$$\tau_{\max} = \frac{T_{\max} \cdot S_y}{2 \cdot a_w \cdot I_y} = \frac{300 \cdot 2424,37}{2 \cdot 0,3 \cdot 166831,87} = 7,27 \frac{\text{кН}}{\text{см}^2}$$

$$\sigma = \tau_{\max} \Rightarrow V_H = 7,27 \frac{\text{кН}}{\text{см}^2} < 12 \frac{\text{кН}}{\text{см}^2} \Rightarrow \text{УСЛАДАМ } a_w = 3 \text{ мм}$$

БЕЗ СЕ ОСТВАРЮЄ ШАРОВИНА ОД 3 мм И ГОРЕ И ДОЛЕ!

КОМПОНА ВЕРТИКАЛНОГО МОМЕНТА

$$a = 2200 \text{ мм}$$

$$b = 750 \text{ мм}$$

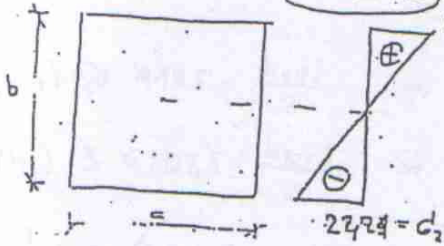
$$d = \frac{a}{b} = 2,933$$

КЛАССА СМР. СБС

$$K_T = 5,34 + \frac{4}{d^2} \Rightarrow \boxed{K_T = 5,80}$$

$$M^* = 1,5 \cdot 660$$

$$T^* = 1,5 \cdot 300 \text{ ПОДПЕРСАНА СИЛА}$$



$$G = \frac{M^*}{I_y} \cdot \frac{b}{2} = \frac{1,5 \cdot 660 \cdot 10^2}{166831,87} \cdot \frac{75}{2} = 22,24 \text{ кН/см}^2$$

$$\gamma = \frac{G_1}{G_2} = \frac{22,24}{-22,24} = -1 \Rightarrow \boxed{K_G = 23,9}$$

$$G_e = \frac{T^* \cdot E}{12(1-\mu^2)} \left( \frac{tw}{b} \right)^2 = \frac{T^* \cdot 21000}{12(1-0,3^2)} \cdot \left( \frac{1}{75} \right)^2 = 3,37$$

$$K_B = 5,98(1-\psi)^2 = 5,98 \cdot 4 = 23,92$$

$$G_{кр} = K_G \cdot G_e = 23,9 \cdot 3,37 = 80,54 \frac{\text{кН}}{\text{см}^2}$$

$$\bar{\lambda}_p = \sqrt{\frac{f_y}{G_{кр}}} = \sqrt{\frac{24}{80,54}} = 0,546 \Rightarrow \lambda_p = \frac{0,6}{\sqrt{\bar{\lambda}_p^2 - 0,13}} = 1,464 \quad \lambda_p = \min(\lambda_p, 1) = 1$$

$$K_G \cdot d^2 = 23,9 \cdot 2,933^2 > 2 \Rightarrow \text{ВАНТИ КРИТЕРИУМ ЧИСТОГ ИЗБОУА СЛАНА } f=0$$

$$\bar{G}_u = (1 - \lambda^2) \cdot \lambda_p + \lambda^2 \cdot \lambda_c \Rightarrow \bar{G}_u = \lambda_p = 1$$

$$C_G = 1,25 - \psi \cdot 0,25 = 1,50 > 1,25 \Rightarrow C_G = 1,25$$

$$G_u = C_G \cdot \bar{G}_u \cdot f_y = 1,25 \cdot 1 \cdot 24 = 30 \frac{\text{кН}}{\text{см}^2} = G_{u, \text{доп}}$$

$$G^* = 22,24 < G_u = 30 \frac{\text{кН}}{\text{см}^2} \Rightarrow \text{СТАБИЛЬНОСТ ЗАДОВОЛЕНА}$$

$$\tau_{кр} = K_T \cdot G_e = 5,80 \cdot 3,37 = 19,55 \frac{\text{кН}}{\text{см}^2}$$

$$\bar{\lambda}_p = \sqrt{\frac{f_y}{\tau_{кр}}} = \sqrt{\frac{24}{19,55}} = 0,842 \Rightarrow \lambda_p = \frac{0,6}{\sqrt{\bar{\lambda}_p^2 - 0,13}} = 0,788 < 1$$

$$\tau_u = C_T \cdot \lambda_p \cdot \frac{f_y}{\sqrt{3}} = 1,25 \cdot 0,788 \cdot \frac{24}{\sqrt{3}} = 13,65 \frac{\text{кН}}{\text{см}^2}$$

$$\tau_{u, \text{доп}} = \min(\tau_u, \frac{f_y}{\sqrt{3}}) \Rightarrow \tau_{u, \text{доп}} = 13,65 \frac{\text{кН}}{\text{см}^2}$$

$$\tau^* = \frac{T^*}{h \cdot tw} = \frac{1,5 \cdot 300}{75 \cdot 1} = 6 \frac{\text{кН}}{\text{см}^2}$$

$$\tau^* = 6 < \tau_{u, \text{доп}} = 13,65 \frac{\text{кН}}{\text{см}^2} \Rightarrow \text{СТАБИЛЬНОСТ ЗАДОВОЛЕНА !}$$

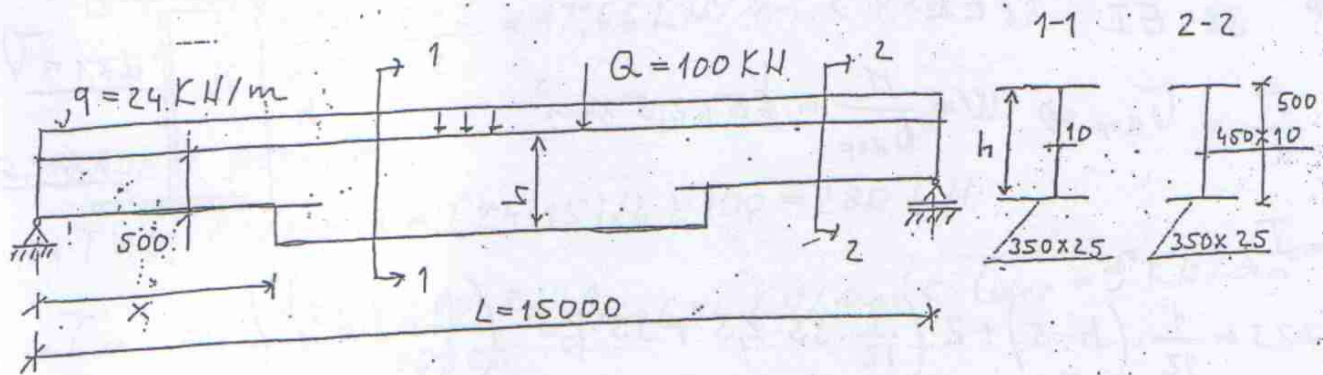
КОНТРОЛ УПОРЕДНОГ КАПОНА :

$$\left( \frac{G^*}{G_u} \right)^2 + \left( \frac{\tau^*}{\tau_u} \right)^2 < 1 \Rightarrow \left( \frac{22,24}{30} \right)^2 + \left( \frac{6}{13,65} \right)^2 = 0,742 < 1$$



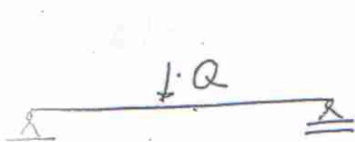
15 APRIL 2008

Q - POKRETHNA SILA

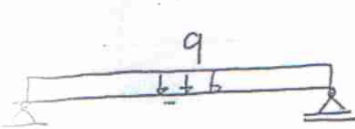


S 235, }  $\Rightarrow \tau_{dop} = 16 \text{ kN/cm}^2 \quad \bar{L}_{dop} = 9 \text{ kN/cm}^2$   
 - SL. OPT

$f_{dop} = L / 500 = 1500 / 500 = 3 \text{ cm}$



$M(x) = \frac{Q \cdot (l-x) \cdot x}{l}$



$M(x) = \frac{q \cdot l}{2} \cdot x - \frac{1}{2} q x^2$

$\frac{Q}{l} \cdot (l-x) \cdot x + \frac{q \cdot l}{2} \cdot x - \frac{1}{2} q x^2$

$x) = \frac{Q}{l} \cdot (l-2x) + \frac{q \cdot l}{2} - q \cdot x = 0 \Rightarrow x = 7,5 \text{ m} \quad \max M = 1050 \text{ kNm}$

DOVNI PRESEK (2-2)

$= \frac{1}{12} \cdot 45^3 + 2 \cdot 2,5 \cdot 35 \cdot 23,75^2 = 106305 \text{ cm}^3$

$= 2,5 \cdot 35 \cdot 23,75 + \frac{45^2}{8} = 2331 \text{ cm}^3$

$= 4252 \text{ cm}^3$

$W_x \cdot \tau_{dop} = 4252 \cdot 16 = 680,35 \text{ kNm}$

- POTREBNA VISINA NOSAČA  $h$  NA SREDINI ( $M=1050 \text{ KNm}$ )

$$f_{\text{dop}} = \frac{5 q l^4}{384 EI} + \frac{Q l^3}{48 EI} = 3 \Rightarrow I_1 \geq 362723 \text{ cm}^4$$

$$\sigma = \frac{M}{W} = \sigma_{\text{dop}} \Rightarrow W = \frac{M}{\sigma_{\text{dop}}} = 6562,5 \text{ cm}^3$$

$$I_1 = I_2 = \dots$$

$$62723 = \frac{1}{12} \cdot (h-5)^3 + 2 \cdot \left( \frac{1}{12} \cdot 35 \cdot 2,5^3 + 35 \cdot 2,5 \cdot \left( \frac{h}{2} - 1,25 \right)^2 \right)$$

$$\Rightarrow \frac{1}{12} \cdot (h-5)^3 + 91,146 + 175 \cdot \left( \frac{h}{2} - 1,25 \right)^2 - 362723 = 0$$

$$\frac{1}{12} (h-5)^3 + 175 \cdot \left( \frac{h}{2} - 1,25 \right)^2 - 362631,85 = 0 \Rightarrow h \geq 87,475 \text{ cm}$$

SVAJA SE:  $h = 87,5 \text{ cm} = 875 \text{ mm}$

$$\left. \begin{aligned} I_x &= 362723 \text{ cm}^4 \\ W_x &= 8291 \text{ cm}^3 \end{aligned} \right\} (1-1)$$

TEORIJSKI I STVARNI POČETAK ODJAČANJA NOSAČA

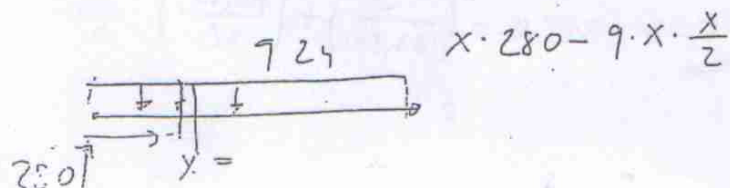
$$0,35 = \frac{100}{15} \cdot (15-x) \cdot x + \frac{24 \cdot 15}{2} \cdot x - \frac{1}{2} \cdot 24 \cdot x^2$$

$$0,35 = 100x - \frac{100}{15} x^2 + 180x - 12x^2$$

$$-15x + 36,447 = 0 \Rightarrow x_{1,2} = \frac{15 \pm \sqrt{15^2 - 4 \cdot 36,447}}{2} = \begin{cases} x_1 = 11,95 \text{ m} \\ x_2 = 3,05 \text{ m} \end{cases}$$

$$x_{\text{STV}_1} = 3,05 - \frac{0,35}{2} = 2,875 \text{ m} \quad \text{USV} \quad \boxed{x_{\text{STV}_1} = 2,85 \text{ m}}$$

$$x_{1,2} = 11,95 + \frac{0,35}{2} = 12,125 \text{ m} \quad \text{USV} \quad \boxed{x_{\text{STV}_2} = 12,15 \text{ m}}$$



# ② KONTROLE NAPONA U KARAKTERISTIČNIM PRESECIMA

\* SREDINA NOSAČA \*

$$\sigma = \frac{M}{W} = \frac{1050 \cdot 10^2}{362723} \cdot \frac{87,5}{2} = 12,66 \text{ KN/cm}^2 < \sigma_{dop} = 16 \text{ KN/cm}^2$$

\* KRAJEVI NOSAČA \*

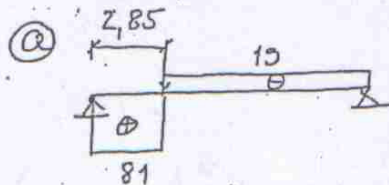
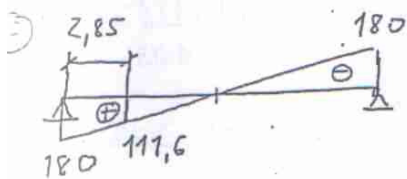
$$\max T = (q \cdot l) / 2 + Q = (24 \cdot 15) / 2 + 100 = 280 \text{ KN}$$

$$\max \tau = \frac{\max T \cdot S_x}{I_x \cdot t_w} = \frac{280 \cdot 2331}{106305 \cdot 1} = 6,14 \text{ KN/cm}^2 < \tau_{dop} = 9 \text{ KN/cm}^2$$

\* MESTO ODJACANJA \*

$$M(2,85) = \frac{100}{15} \cdot (15 - 2,85) \cdot 2,85 + \frac{24 \cdot 15}{2} \cdot 2,85 - \frac{1}{2} \cdot 24 \cdot 2,85^2 = 646,38 \text{ KNm}$$

$$T(2,85) = 111,6 + 81 = 192,6 \text{ KN}$$



$$\sigma_1 = \frac{646,38 \cdot 10^2}{106305} \cdot 22,5 = 13,68 \text{ KN/cm}^2$$

$$\tau_1 = \frac{192,6 \cdot 2,5 \cdot 35 \cdot 23,75}{106305 \cdot 1} = 3,77 \text{ KN/cm}^2$$

$$\sigma_w = \sqrt{13,68^2 + 3 \cdot 3,77^2} = 15,14 \text{ KN/cm}^2 < \sigma_{dop} = 16 \text{ KN/cm}^2$$

✓ BORAVIČENO !!!

✓ UPOREDNI NAPON NA SREDINI NOSAČA \*

$$\sigma = \frac{1050 \cdot 10^2}{362723} \cdot 41,25 = 11,94 \text{ KN/cm}^2$$

$$\tau = \frac{50 \cdot 2,5 \cdot 35 \cdot 42,5}{362723 \cdot 1} = 0,51 \text{ KN/cm}^2$$

$$\sigma_w = \sqrt{11,94^2 + 3 \cdot 0,51^2} = 11,97 \text{ KN/cm}^2 < \sigma_{dop}$$



# KONTROLA UGIBA NOSAČA

$$= \frac{5 \cdot q \cdot l^3}{384 \cdot EI} + \frac{Q \cdot l^3}{48 EI} = \frac{5 \cdot 24 \cdot 1500^3 \cdot 10^{-2}}{384 \cdot 21000 \cdot 362723} + \frac{100 \cdot 1500^3}{48 \cdot 21000 \cdot 362723} = 3 \text{ cm}$$

$$h = 87,8 \text{ mm}$$



$$I_x = 362723 \text{ cm}^4$$

$$I_y = 3159 \text{ cm}^4$$

$$0,35 = \frac{100}{15} \cdot (15 \cdot x) + \frac{24 \cdot 15^3}{15} \cdot x$$

$$0,35 = 100x - \frac{24 \cdot 15^3}{15} \cdot x$$

$$457 + 35,447 = 0 \Rightarrow x = \frac{457 + 35,447}{15}$$

$$x = 31,5 \text{ mm}$$

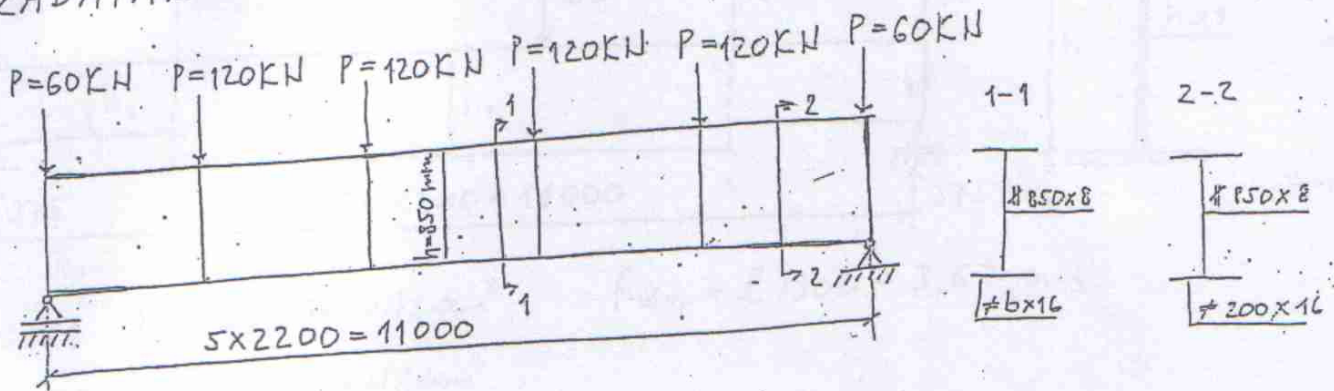
$$x = 31,5 \text{ mm}$$

$$x = 31,5 \text{ mm}$$

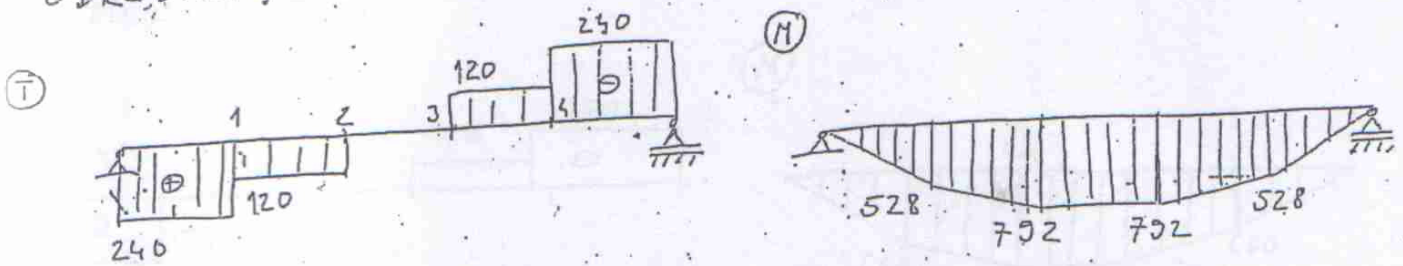
19. JAN 2004

(1)

1. ZADATAK Č. 0361 I SL. OPT  $\Rightarrow \bar{\sigma}_{dop} = 16 \text{ KN/cm}^2$   $\bar{\tau}_{dop} = 9$



- ODREĐIVANJE POTREBNE ŠIRINE OJAČANE NOŽICE



PRESEK 1-1

$$I_x = \frac{1}{12} \cdot 85^3 \cdot 0,8 + 2 \cdot b \cdot 1,6 \left( \frac{85}{2} + 0,8 \right)^2 = 40041,67 + 6000b \quad (I_x = 220952 \text{ cm}^4)$$

$$W_x = \frac{40041,67 + 6000b}{44,1} = 928,38 + 136,05b$$

$$\bar{\sigma}_{dop} = 16 \geq \frac{m \cdot x \cdot M}{W_x} = \frac{792 \cdot 100}{928,38 + 136,05b} \Rightarrow b \geq 20,56 \text{ cm}$$

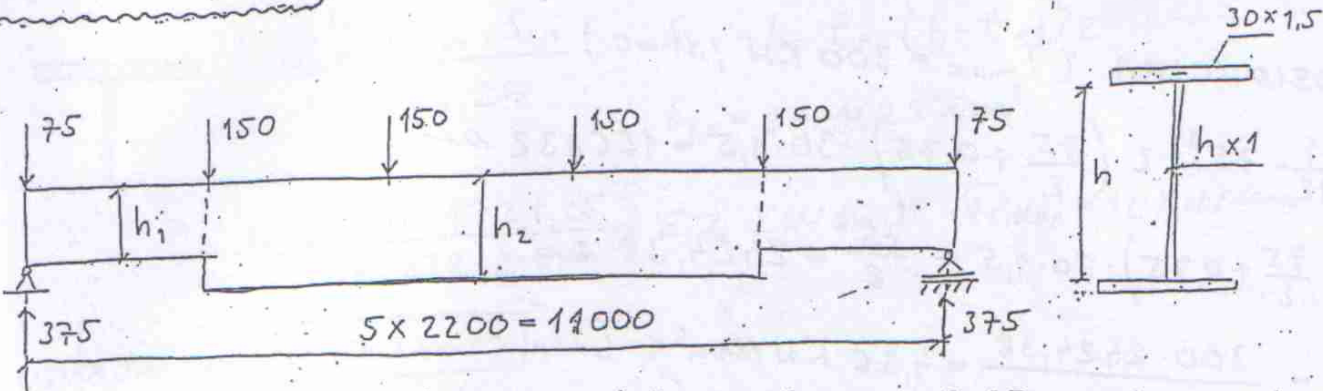
USVAJA SE  $\neq 300 \times 16$  ( $\bar{\sigma} = 15,81 \text{ KN/cm}^2$ )

$$S_x = \frac{85}{2} \cdot 0,8 \cdot \frac{85}{4} + 30 \cdot 1,6 \cdot \left( \frac{85}{2} + 0,8 \right) = 2801 \text{ cm}^3$$

$$\bar{\tau} = \frac{T \cdot S_x}{I_x \cdot t_w} = \frac{120 \cdot 2801}{220952 \cdot 0,8} = 1,9 \text{ KN/cm}^2 < \bar{\tau}_{dop} = 9 \text{ KN/cm}^2$$

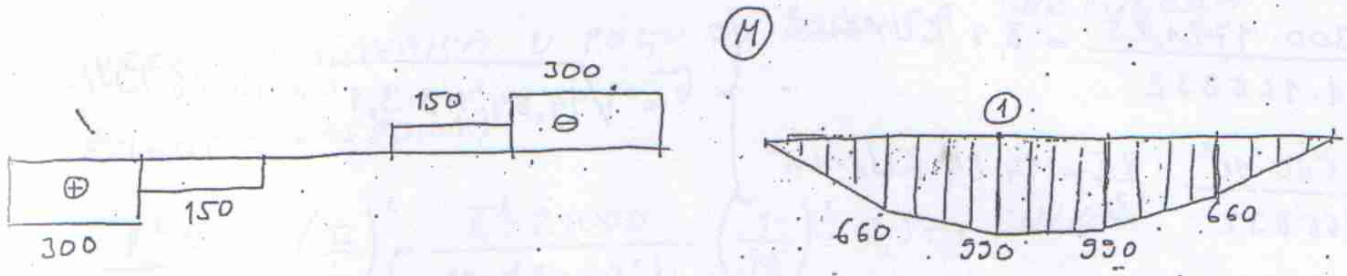
$$\bar{\tau}_w = \sqrt{\bar{\sigma}^2 + 3\bar{\tau}^2} = \sqrt{15,81^2 + 3 \cdot 1,9^2} \approx 16 \text{ KN/cm}^2$$

8. JUL. 2002



C 0361 }  $\sigma_{dop} = 16 \text{ KN/cm}^2$   $f_{dop} = L 1300 = 3,67 \text{ mm}$   
 I SL. OPT. }  $\tau_{dop} = 9 \text{ KN/cm}^2$

STATIČKI UTICAJI:



$$I = \frac{M \cdot h_1}{\sigma_d \cdot z}$$

$$= \frac{1}{12} \cdot h_1^3 + 2 \left( \frac{h_1}{2} + 0,75 \right)^2 \cdot 30 \cdot 1,5 = \frac{660 \cdot 10^2}{16} \left( \frac{h_1}{2} + 1,5 \right)$$

$$\frac{1}{12} h_1^3 + 90 \left( \frac{h_1}{2} + 0,75 \right)^2 - 2062,5 h_1 - 6187,5 = 0$$

$\Rightarrow h_1 = 72,79 \text{ cm}$  USVOJENO  $h_1 = 75 \text{ cm}$  HALO VEĆE ZBOG ZAHEMARENIH TILA

$$= \frac{1}{12} h_2^3 + 2 \cdot \left( \frac{h_2}{2} + 0,75 \right)^2 \cdot 30 \cdot 1,5 = \frac{990 \cdot 10^2}{16} \left( \frac{h_2}{2} + 1,5 \right)$$

$$\frac{1}{12} h_2^3 + 90 \left( \frac{h_2}{2} + 0,75 \right)^2 - 3093,75 h_2 - 9281,25$$

$h_1 = 100,88 \text{ cm}$  USVOJENO  $h_2 = 101 \text{ cm}$  NIJE VEĆE ZBOG TOGA ŠTO ZA  $M_{max}$   $T=0$



### LAPONSKÉ KONTROLE

D OSLOHCIMA ( $T_{max} = 300 \text{ KN}$ ,  $M = 0$ )

$$I_x = \frac{1}{12} \cdot 75^3 + 2 \cdot \left( \frac{75}{2} + 0,75 \right)^2 \cdot 30 \cdot 1,5 = 166832 \text{ cm}^4$$

$$= \left( \frac{75}{2} + 0,75 \right) \cdot 30 \cdot 1,5 + \frac{75^2}{8} = 2424,38 \text{ cm}^3$$

$$\times \tau = \frac{300 \cdot 2424,38}{166832 \cdot 1} = 4,36 \text{ KN/cm}^2 < \tau_{dop}$$

NESTU OJACANJA ( $T = 300 \text{ KN}$ ,  $M = 660 \text{ KNm}$ )

$$= \left( \frac{75}{2} + 0,75 \right) \cdot 30 \cdot 1,5 = 1721,25 \text{ cm}^3 \quad I_x = 166832 \text{ cm}^4$$

$$= \frac{300 \cdot 1721,25}{1 \cdot 166832} = 3,1 \text{ KN/cm}^2$$

$$= \frac{660 \cdot 10^2}{166832} \cdot \frac{75}{2} = 14,84 \text{ KN/cm}^2$$

$$\tau_u = \sqrt{14,84^2 + 3 \cdot 3,1^2} = 15,78 \text{ KN/cm}^2$$

NESTU TACKE ① ( $T = 150 \text{ KN}$ ,  $M = 990 \text{ KNm}$ )

$$I_x = \frac{1}{12} \cdot 101^3 + 20 \cdot \left( \frac{101}{2} + 0,75 \right)^2 = 322249 \text{ cm}^4$$

$$= \left( \frac{101}{2} + 0,75 \right) \cdot 30 \cdot 1,5 = 2306,25 \text{ cm}^3$$

$$= \frac{150 \cdot 2306,25}{322249 \cdot 1} = 1,07 \text{ KN/cm}^2$$

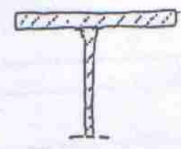
$$= \frac{990 \cdot 10^2}{322249} \cdot \frac{101}{2} = 15,51 \text{ KN/cm}^2$$

$$\tau_u = \sqrt{15,51^2 + 3 \cdot 1,07^2} = 15,62 \text{ KN/cm}^2$$

SREDINI RASPOHA ( $T = 0$ ,  $M = 990 \text{ KNm}$ )

$$= \frac{990 \cdot 10^2}{322249} \cdot \frac{101+3}{2} = 15,98 \text{ KN/cm}^2$$

- UGAONI ŠAVOVI ZA VEZU NOŽICE I REBRA



$$V_{II} = \frac{V_{max} \cdot S_{y,1}}{I_x \cdot 2a}$$

$$S_{y,1} = b_f \cdot t_f \cdot (h - t_f) / 2$$

$$S_{y,1} = 1721,25 \text{ cm}^3$$

$$V_{II} = \frac{300 \cdot 1721,25}{166832 \cdot 2 \cdot 0,3} = 5,2 \text{ KN/cm}^2 < \sqrt{s_{dop}} = 12 \text{ KN/cm}^2$$

USVAJA SE  $a_w = 3 \text{ mm}$

- KONTROLA UGIBA

$$f = \frac{F l^3}{15,87 EI} = \frac{150 \cdot (1100)^3}{15,87 \cdot 21000 \cdot 322249} = 1,86 \text{ cm} < f_{dop}$$

PROVERA IZBOČAVANJA U POLJU DO OSLOHCA (UKRUCENJA U PETINAMA RASPOHA)

$$\tau_E = \frac{\pi^2 E}{12 \cdot (1 - \nu^2)} \cdot \left(\frac{t}{b}\right)^2 = \frac{\pi^2 \cdot 21000}{12 \cdot (1 - 0,3^2)} \cdot \left(\frac{1}{75}\right)^2 = 3,374 \text{ KN/cm}^2$$

$$\lambda = a/b = 22/0,75 = 2,933 > 1 \quad K_\tau = 5,34 + \frac{4}{\lambda^2} = 5,34 + \frac{4}{2,933^2} = 5,805$$

$$K_\sigma = 23,9$$

$$\sigma_{kr} = \tau_E \cdot K_\sigma = 23,9 \cdot 3,374 = 80,64 \text{ KN/cm}^2$$

$$\tau_{kr} = \tau_E \cdot K_\tau = 5,805 \cdot 3,374 = 19,59 \text{ KN/cm}^2$$

$$\bar{\lambda}_{\rho\sigma} = \sqrt{f_y / \sigma_{kr}} = \sqrt{24 / 80,64} = 0,546 \quad \bar{\lambda}_{\rho\tau} = \sqrt{f_y / (\sqrt{3} \cdot \tau_{kr})} = \sqrt{24 / (\sqrt{3} \cdot 19,59)} = 0,841$$

$$\chi_\sigma = \frac{0,6}{\sqrt{\bar{\lambda}_{\rho\sigma}^2 - 0,13}} = \frac{0,6}{\sqrt{0,546^2 - 0,13}} = 1,463 \quad \chi_\tau = \frac{0,6}{\sqrt{0,841^2 - 0,13}} = 0,79$$

$$\chi_\tau = \min(1, \chi_\tau)$$

$$\chi_\sigma = \min(1, \chi_\sigma)$$

$$\alpha = C_T \chi_\tau \cdot f_y / \sqrt{3} \quad C_T \text{ JE UVEK } 1,25 !!!$$

$$= 1,25 \cdot 0,79 \cdot 24 / \sqrt{3} = 13,68 \text{ KN/cm}^2 < f_y / \sqrt{3} = 13,86$$

$$\tau = \underbrace{(1,5)}_{\substack{\text{KOE.F.} \\ \text{SIGURN.}}} \frac{300 \cdot 1721,25}{166832 \cdot 1} = 4,64 \text{ KN/cm}^2 < \tau_u \quad (T^* = 1,5T)$$

$$C = 2 - \frac{\sigma_{cr}}{\sigma_c} \quad \sigma_c = \frac{\sigma_E}{\alpha^2} \quad \sigma_{cr} = K_{\sigma} \cdot \sigma_E$$

$$C = 2 - \frac{K_{\sigma} \cdot \sigma_E}{\sigma_E / \alpha^2} = 2 - 23,3 \cdot 2,033 < 0 \Rightarrow f = 0$$

$$\sigma = 1,25 - 0,25 \psi = 1,25 - (-1) \cdot 0,25 = 1,5 > 1,25 \Rightarrow \text{USV. } C_{\sigma} = 1,25$$

$$\bar{\sigma}_w = (1 - f^2) \cdot \chi_{p0} + f \cdot \chi_c \Rightarrow \bar{\sigma}_w = \chi_{p0} = 1$$

$$\bar{\sigma}_{ux} = C_{\sigma} \cdot \bar{\sigma}_w \cdot f_y = 1,25 \cdot 1 \cdot 24 = 30 > \bar{\sigma}_{dop} = 24 \Rightarrow \bar{\sigma}_{ux} = 24 \text{ KN/cm}^2$$

$$\tau = 1,5 \cdot \frac{660 \cdot 10^2}{166832} \cdot \frac{75}{2} = 1,5 \cdot 14,83 = 22,25 < \bar{\sigma}_{ux}$$

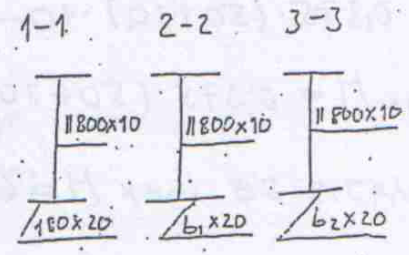
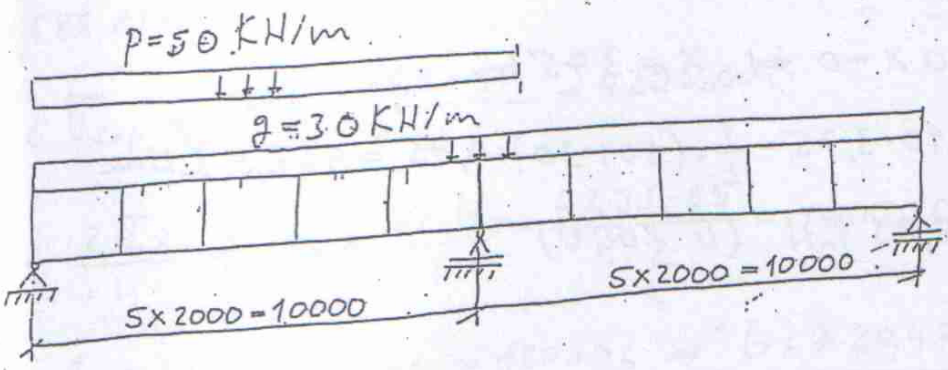
1. POREDNI

$$\left( \frac{\sigma_x}{\bar{\sigma}_{ux}} \right)^2 + \left( \frac{\tau}{\tau_u} \right)^2 = \left( \frac{22,25}{24} \right)^2 + \left( \frac{4,64}{13,68} \right)^2 = 0,975 < 1$$



03. OKTOBAR 2004

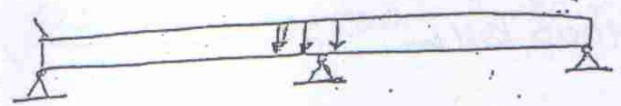
1



$\bar{c} 0361$   
 I SL. OPT }  $\Rightarrow \bar{\sigma}_{dop} = 16 \text{ KN/cm}^2$      $\bar{\tau}_{dop} = 9 \text{ KN/cm}^2$

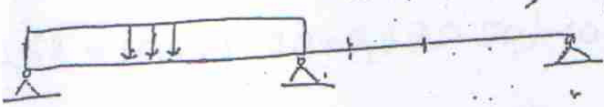
MAX. UTICAJI

g)



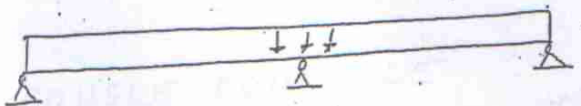
$M_q(x) = 0,375 q l x - \frac{1}{2} q x^2$

p) NA POLA



$M_p(x) = 0,438 p l x - \frac{1}{2} p x^2$

p) NA CITAVOM



$M_p(x) = 0,375 p l x - \frac{1}{2} p x^2$

- DELUJU q i p NA POLA

$M = (0,375 q l + 0,438 p l) x - \frac{1}{2} (q + p) x^2$

$0,375 \cdot 3 \cdot 10 + 0,438 \cdot 5 \cdot 10 - 8x = 0 \Rightarrow x = 4,14 \text{ m}$

$\max M = (0,375 \cdot 30 + 0,438 \cdot 50) \cdot 10 \cdot 4,14 - \frac{1}{2} \cdot (50 + 30) \cdot 4,14^2 = 686,83 \text{ KNm}$

$\max M = 686,83 \text{ KNm}$  (MOMENT U POLU)

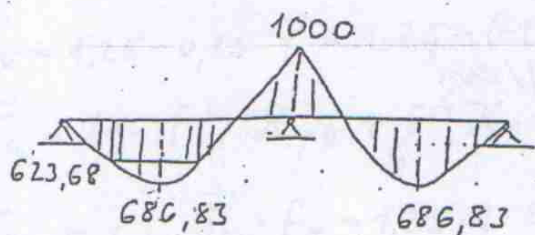
DELUVU P i g

$$V = 0,375 \cdot (q+p) \cdot lx - \frac{1}{2} (q+p) x^2$$

$$0,375 \cdot (50+30) \cdot 10 - 80x = 0 \Rightarrow x = 3,75 \text{ m}$$

$$\max M = 0,375 \cdot (50+30) \cdot 10 \cdot 3,75 - \frac{1}{2} \cdot (50+30) \cdot 3,75^2 = 562,5 \text{ KNm}$$

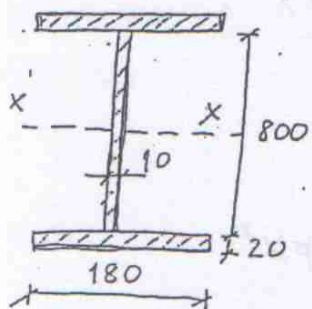
SVAJA SE  $\max M = 686,83 \text{ KN}$  (U POLJU)



PRESEK NA D OSLOHCEM

$$\min M = (0,125 \cdot 30 + 0,125 \cdot 50) \cdot 10^2 = 1000 \text{ KNm}$$

SHOVNI PRESEK



$$I_x = 163723 \text{ cm}^4$$

$$S_x = 2276 \text{ cm}^3$$

$$A = 152 \text{ cm}^2$$

$$W_x = 3898 \text{ cm}^3$$

$$\sigma_s = W_x \cdot \sigma_{dop} = 3898 \cdot 16 = 623,68 \text{ KNm}$$

$$623,68 = (0,375 \cdot 30 + 0,375 \cdot 50) \cdot 10 \cdot x - \frac{1}{2} \cdot (30+50) \cdot x^2$$

$$8,2875x + 15,592 = 0 \Rightarrow x_1 = 2,887 \text{ m} \quad x_2 = 5,4 \text{ m}$$

$$x_1 = 2,887 - \frac{0,21}{2} = 2,782 \text{ m} \quad \text{USVAJA SE } \boxed{x_{stv,1} = 2,75 \text{ m}} \quad \left. \begin{array}{l} \text{PRESEK} \\ \text{U POLJU} \end{array} \right\}$$

veće br

$$x_2 = 5,4 + \frac{0,21}{2} = 5,49 \text{ m} \quad \text{USVAJA SE } \boxed{x_{stv,2} = 5,5 \text{ m}}$$

ESEK 2-2

$$686,83 \text{ KNm}$$

$$\leq \sqrt{\sigma_{\text{dop}}} \Rightarrow W \geq \frac{686,83 \cdot 10^2}{16} = 4293 \text{ cm}^3$$

$$= \frac{2 I_x}{h} \Rightarrow I_x \geq \frac{W \cdot h}{2} = \frac{4293 \cdot 84}{2} = 180306 \text{ cm}^4$$

$$= \frac{1}{12} \cdot 80^3 \cdot 1 + 2 \cdot 2 \cdot b_f \cdot 41^2 = 180306 \Rightarrow b_f \geq 20,47 \text{ cm}$$

$$\text{USV } b_f = 21 \text{ cm}$$

ESEK 3-3

$$\geq \frac{1000 \cdot 10^2}{16} = 6250 \text{ cm}^3$$

$$\geq \frac{6250 \cdot 84}{2} = 262500 = \frac{1}{12} \cdot 80^3 + 2 \cdot 2 \cdot b_f \cdot 41^2 \Rightarrow b_f \geq 32,86 \text{ cm}$$

$$\text{USV } b_f = 40 \text{ cm}$$

ŠTO OĐAČANJA BLIZU SREDNJEG OSLOHCA

$$23,68 = (0,375 \cdot 30 + 0,375 \cdot 50) \cdot 10 \cdot x - \frac{1}{2} \cdot (50 + 30) \cdot x^2$$

$$7,5 - 15,5x^2 = 0 \Rightarrow x = 0,196 \text{ m}$$

$$v = 0,196 - \frac{0,4}{2} = 8,996 \text{ m} \Rightarrow \text{USV } x_{\text{STVR}} = 9 \text{ m}$$

(APOHSKE KONTROLE

A MESTU MAX. MOMENTA U POLJU \* (PRESEK 2-2)

$$= \frac{1}{12} \cdot 80^3 \cdot 1 + 2 \cdot 2 \cdot 21 \cdot 41^2 + 2 \cdot \frac{1}{12} \cdot 21 \cdot 2^3 = 183899 \text{ cm}^4$$

$$= \frac{686,83 \cdot 10^2}{183899} \cdot \frac{84}{2} = 15,69 \text{ KN/cm}^2 < \sqrt{\sigma_{\text{dop}}}$$

I KRAJNJEI OSLOHCU \* (PRESEK 1-1) (T = 331,5 KN)

$$\frac{T \cdot S_x}{I_x \cdot t_w} = \frac{331,5 \cdot 2276}{163723 \cdot 1} = 4,61 \text{ KN/cm}^2 < T_{\text{dop}}$$



\* U SREDNEM OSLONCU \* ( $T = 500 \text{ KN}$   $M = 1000 \text{ KNm}$ )

$$x = \frac{1}{12} \cdot 80^3 \cdot 1 + 2 \left( \frac{1}{12} \cdot 40 \cdot 2^3 + 40 \cdot 2 \cdot 41^2 \right) = 311680 \text{ cm}^4$$

$$\bar{\tau} = \frac{1000 \cdot 10^2 \cdot 40}{311680} = 12,83 \text{ KN/cm}^2$$

$$S_x^o = 2 \cdot 40 \cdot 41 = 3280 \text{ cm}^3$$

$$\tau = \frac{T \cdot S_x^o}{I_x \cdot t_w} = \frac{500 \cdot 3280}{311680 \cdot 1} = 5,26 \text{ KN/cm}^2$$

$$u = \sqrt{\bar{\tau}^2 + \tau^2} = \sqrt{12,83^2 + 3 \cdot 5,26^2} = 15,74 \text{ KN/cm}^2 < \bar{\tau}_{\text{dop}}$$

DIMENZIONISANJE ŠAVOVA ZA VEZU REBRA I GORNJE I DOĐE NOŽICE

$$3 \text{ mm} \leq a_w \leq 7 \text{ mm}$$

ISVAĐA SE  $a_w = 3 \text{ mm}$

$$u = \frac{\max V \cdot S_x^o}{I_x \cdot 2 \cdot a_w} = \frac{500 \cdot 3280}{311680 \cdot 2 \cdot 0,3} = 8,77 \text{ KN/cm}^2 < \bar{\tau}_{s, \text{dop}} = 12 \text{ KN/cm}^2$$

A KRAJNJI OSLOHAC \*

$$= \frac{331,5 \cdot 18 \cdot 2 \cdot 41}{163723 \cdot 2 \cdot 0,3} = 4,98 \text{ KN/cm}^2 < \bar{\tau}_{s, \text{dop}}$$

CONTROLA STABILNOSTI NOSAČA NA BOČNO TORZIJSKO IZVIJANJE

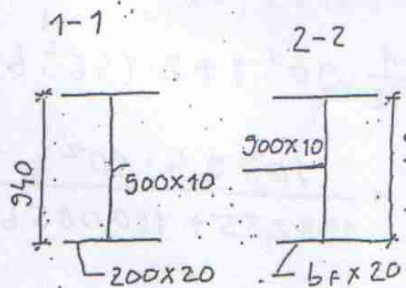
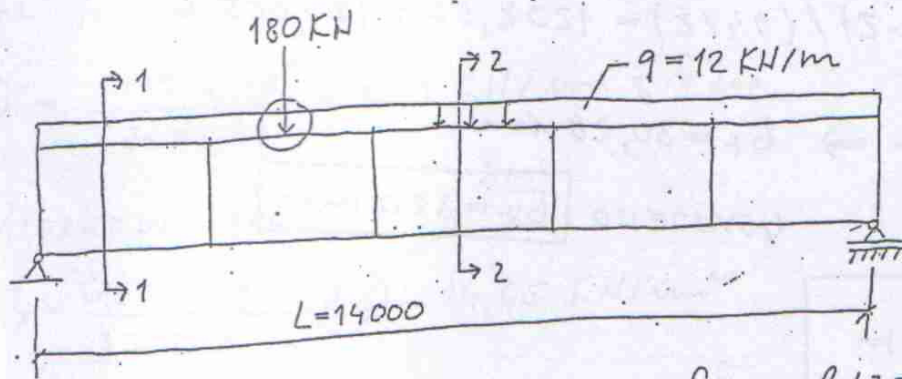
$$= 200 \text{ cm}$$

$$= \sqrt{\frac{\frac{1}{12} \cdot 18^3 \cdot 2}{21 \cdot 2}} = \frac{18}{\sqrt{12}} = 5,196 \text{ cm}$$

$$= \frac{l_y}{\bar{l}_y} = \frac{200}{5,196} = 38,49 < 40 \rightarrow \text{NEMA OPASNOSTI OD BOČNO TORZIJSKOG IZVIJANJA}$$

17. JANUAR 2006

VISINA ŠINE  $h = 149 \text{ mm}$

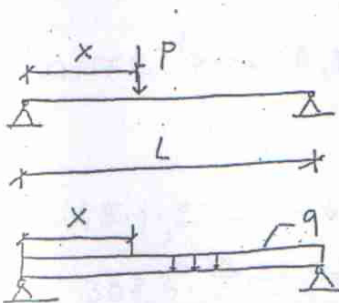


S 235 }  
I-SL.OPT }  $\Rightarrow \begin{cases} \sigma_{dop} = 16 \text{ kN/cm}^2 \\ \tau_{dop} = 9 \text{ kN/cm}^2 \end{cases} \quad f_{dop} = l/300 = 4,67 \text{ cm}$

NOSAČ JE BOČNO PRIDRŽAN NA SVAKIH 2800 mm

$\psi = 1,1$  - KOEF. IZRAVNAVA (ZA STATIČKO OPTEREĆENJE)

$\varphi = 1,2$  - KOEF. IZRAVNAVA (ZA DINAMIČKO OPTEREĆENJE)



$$M(x) = 1,2 \cdot \frac{P \cdot (L-x)}{L} \cdot x = 15,43 x (14-x)$$

$$M(x) = 1,1 \cdot \frac{q}{2} x (L-x) = 6,6 x (14-x)$$

$$M(x) = 20,7 x (14-x)$$

$$M(x) = 1,2 \cdot \frac{P \cdot (L-x)}{L} \cdot x + 1,1 \cdot \frac{q}{2} x (L-x)$$

$$\max M = M(7) = 1,2 \cdot \frac{180 \cdot 7}{14} \cdot 7 + 1,1 \cdot 6 \cdot 7 \cdot 7 = 1079,4 \text{ kNm}$$

$$I_1 = \frac{1}{12} 30^3 + 2 \cdot (46^2 \cdot 20 \cdot 2) = 230030 \text{ cm}^4 \quad W_1 = \frac{2I_1}{h} = 4894,25 \text{ cm}^3$$

$$\varphi_{nos} = 16 \cdot 4894,25 \cdot 10^{-2} = 783,08 \text{ kNm}$$

$$-83,08 = 1,2 \cdot \frac{180 \cdot (14-x)}{14} \cdot x + 1,1 \cdot 6 \cdot x \cdot (14-x) = 216x - 15,429x^2 + 92,4x - 6,6x^2$$

$$-14x + 35,55 = 0 \quad x_{1,2} = \frac{14 \pm \sqrt{14^2 - 4 \cdot 35,55}}{2} = \begin{cases} 10,67 \text{ m} \\ 3,33 \text{ m} \end{cases}$$

SREDINU (max H)

$$I = \frac{1}{12} \cdot 90^3 \cdot 1 + 2 \cdot (46^2 \cdot b_f \cdot 2) / (94/2) = 1292,55 + 180,085 b_f$$

$$16 = \frac{1079,4 \cdot 10^{-2}}{1292,55 + 180,085 b_f} \Rightarrow b_f = 30,28 \text{ cm}$$

USVOJENO  $b_f = 320 \text{ mm}$

$$s_{TV} = 3,33 - \frac{0,32}{2} = 3,17 \text{ m}$$

$$s_{TV} = 10,67 + \frac{0,32}{2} = 10,83 \text{ m}$$

4 PONSKE KONTROLE

POK USLED LOKALNOG PRITISKA TOČKA

$$F = 3,2^3 \sqrt{\frac{I_{y,f}}{t_w}} \quad \text{ZA } h = 149 \text{ mm} \Rightarrow I_{y,s} = 1819 \text{ cm}^4$$

$$\text{E OJAČANJA} \quad I_{y,f} = I_{y,s} + \frac{2^3 \cdot 20}{12} = 1819 + 13,33 = 1832,33 \text{ cm}^4$$

$$b_{eff} = 3,2^3 \sqrt{\frac{1832,33}{1}} = 39,16 \text{ cm}$$

$$\text{SLE OJAČANJA} \quad I_{y,f} = I_{y,s} + \frac{2^3 \cdot 32}{12} = 1819 + 21,33 = 1840,33 \text{ cm}^4$$

$$b_{eff} = 3,2^3 \sqrt{\frac{1840,33}{1}} = 39,21 \text{ cm}$$

$$\tau = \frac{F \cdot P}{b_{eff} \cdot t_w}$$

$$\text{RE OJAČANJA} \quad \sqrt{\tau} = \frac{1,2 \cdot 180}{39,16 \cdot 1} = 5,52 \text{ KN/cm}^2$$

$$\text{SLE OJAČANJA} \quad \sqrt{\tau} = \frac{1,2 \cdot 180}{39,21 \cdot 1} = 5,51 \text{ KN/cm}^2$$



③  
KONTROLA NA  $\max M = 1079,4 \text{ KNm}$  odg  $T = 1,2 \cdot 90 = 108 \text{ KN}$

$$I_z = \frac{1}{12} \cdot 90^3 + 2 \cdot (32 \cdot 2 \cdot 46^2) = 331598 \text{ cm}^4 \quad W_1 = \frac{2I_z}{h} = 7055,28 \text{ cm}^3$$

$$\sigma = \frac{1079,4 \cdot 10^2}{7055,28} = 15,3 \text{ KN/cm}^2 < \sigma_{\text{dop}}$$

UPOREDNI NAPON  $\rightarrow \frac{h_{\text{reč}}}{2}$

$$\sigma_x = \frac{1079,4 \cdot 10^2}{331598} \cdot 45 = 14,65 \text{ KN/cm}^2$$

$$S_{x,0} = 32 \cdot 2 \cdot 46 = 2944 \text{ cm}^3$$

$$\sigma_z = 5,51 \text{ KN/cm}^2$$

$$\tau_{xz} = \frac{108 \cdot 2944}{331598} \cdot 1 = 0,96 \text{ KN/cm}^2 \rightarrow t_w$$

$$\tau_{zx} = 0,2 \cdot \sigma_z = 1,102 \text{ KN/cm}^2$$

$$\sigma_u = \sqrt{\sigma_x^2 + \sigma_z^2 - \sigma_x \sigma_z + 3(\tau_{xz} + \tau_{zx})^2} =$$

$$= \sqrt{14,65^2 + 5,51^2 - 14,65 \cdot 5,51 + 3 \cdot (0,96 + 1,102)^2} = 13,3 \text{ KN/cm}^2$$

KONTROLA NAD OSLOHCEM  $M=0$

$$T = 1,2 \cdot 180 + 1,1 \cdot 12 \cdot 14/2 = 308,4 \text{ KN}$$

$$S = 45 \cdot 1 \cdot 22,5 + 46 \cdot 20 \cdot 2 = 2852,5 \text{ cm}^3$$

$$\tau = \frac{308,4 \cdot 2852,5}{230030 \cdot 1} = 3,82 \text{ KN/cm}^2 < \tau_{\text{dop}}$$

KONTROLA NA MESTU OJAČANJA

$$T(3,17) = 1,2 \cdot \frac{180 \cdot (14 - 3,17)}{14} \cdot 3,17 + 1,1 \cdot 6 \cdot 3,17 \cdot (14 - 3,17) = 756,27 \text{ KNm}$$

$$\Gamma(3,17) = 1,2 \cdot \frac{180 \cdot (14 - 3,17)}{14} + 1,1(12 \cdot 7 - 12 \cdot 3,17) = 217,65 \text{ KN}$$

$$\sigma_x = \frac{756,27 \cdot 10^2}{230030} \cdot 45 = 14,79 \text{ KN/cm}^2$$

$$\tau_{xz} = \frac{217 \cdot 20 \cdot 2 \cdot 46}{230030 \cdot 1} = 1,74 \text{ KN/cm}^2$$

$$\sigma_z = 5,52 \text{ KN/cm}^2 \quad \tau_{zx} = 0,2 \sigma_z = 1,104 \text{ KN/cm}^2$$

$$\sigma_u = \sqrt{\sigma_x^2 + \sigma_z^2 - \sigma_x \cdot \sigma_z + 3 \cdot (\tau_{xz} + \tau_{zx})^2}$$

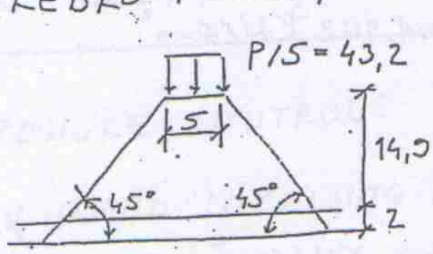
$$= \sqrt{14,79^2 + 5,52^2 - 14,79 \cdot 5,52 + 3 \cdot (1,74 + 1,104)^2} = 13,85 \text{ KN/cm}^2 < \sigma_{dop}$$

KONTROLA UGIBA NOSAČA

$$f = \frac{1,2 \cdot 180 \cdot (1400)^3}{48 \cdot 21000 \cdot 331589} + 1,1 \cdot \frac{5 \cdot 12 \cdot (1400)^4 \cdot 10^{-2}}{384 \cdot 21000 \cdot 331589} = 2,72 \text{ cm} < f_{dop}$$

DIMENZIONISANJE ŠAVOVA ZA VEŽU REBRA I GORNJE, DOHNE NOŽICE.

REBRO I GORNJA NOŽICA



$$l_w = 2 \cdot (14,7 + 2) + 5 = 38,8 \text{ cm}$$

$$V_{max} = 308,4 \text{ KN} \quad V_{max} = 200,4 \text{ KN}$$

$$S_{y,0} = 20 \cdot 2 \cdot 46 = 1840 \text{ cm}^3$$

$$V_{II} = \frac{V_{max} \cdot S_{y,0}}{I_y \cdot 2a_w} = \frac{308,4 \cdot 1840}{230030 \cdot 2 \cdot a_w} = \frac{1,233}{a_w} = \frac{0,3015}{a_w}$$

$$\eta = \frac{P}{2l_w \cdot a_w} = \frac{1,2 \cdot 180}{2 \cdot 38,8 \cdot a_w} = \frac{2,784}{a_w}$$

$$\sigma_u = \sqrt{V_{II}^2 + \eta^2} = \sqrt{\left(\frac{2,784}{a_w}\right)^2 + \left(\frac{1,233}{a_w}\right)^2} < \sigma_{dop} \Rightarrow a_w \geq 0,25 \text{ cm}$$

USVAJA SE  $2 \times a_w = 3 \text{ mm}$

KONTROLA NA BOČNO-TORČ. IZMIRNANJE NOSAČA

$$= 20 \text{ cm}, \quad I_{zf} = \frac{32^3 \cdot 2}{12} = 5461,33 \text{ cm}^4$$

$$I = 2 \cdot 32 = 64 \text{ cm}^2$$

$$f = \sqrt{\frac{5461,33}{64}} = 9,230 \text{ cm}$$

$$\frac{200}{9,230} = 30,3 < 40 \text{ nema oštećenja}$$